

Given $g(x) = \sqrt{6x^4 + 11x^2}$, use the derivative rule for inverse functions to determine $(g^{-1})'(g(-2))$.

$$g^{-1}[g(x)] = x,$$

$$(g^{-1})'[g(x)] \cdot g'(x) = 1 \quad \text{So}$$

$$(g^{-1})'[g(x)] = \frac{1}{g'(x)}. \quad \text{Now}$$

$$g'(x) = \frac{1}{2\sqrt{6x^4 + 11x^2}} (24x^3 + 22x)$$

$$g'(-2) = \frac{-168}{\sqrt{140}}. \quad \text{So}$$

$$(g^{-1})'(g(-2)) = \frac{1}{g'(-2)} = \frac{-\sqrt{140}}{168}.$$